

Inferring Cognitive Models from Data using Approximate Bayesian Computation

CHI 2017

Antti Kangasräsiö¹, Kumaripaba Athukorala¹, Andrew Howes²,
Jukka Corander³, Samuel Kaski¹, Antti Oulasvirta⁴

¹Helsinki Institute for Information Technology HIIT,
Department of Computer Science, Aalto University, Finland

²School of Computer Science, University of Birmingham, UK

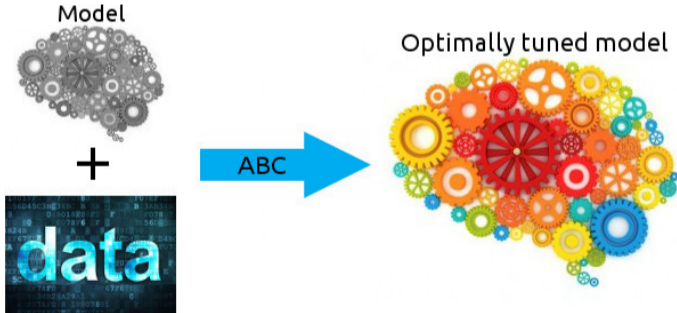
³Department of Biostatistics, University of Oslo, Norway

⁴Helsinki Institute for Information Technology HIIT,
Department of Communications and Networking, Aalto University, Finland

Tuesday 9.5.2017

Main Contribution

Parameters of cognitive models can be tuned based on commonly available observation data using Approximate Bayesian Computation (ABC)



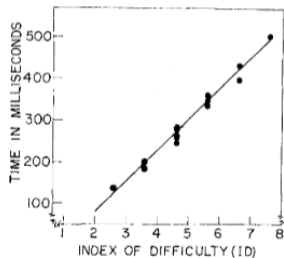
Examples of Cognitive Models

Examples of Cognitive Models

Early work:

Fitt's law (1954)

Speed/accuracy trade-off
in pointing tasks

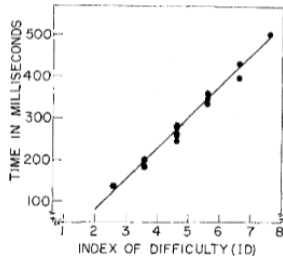


Examples of Cognitive Models

Early work:

Fitt's law (1954)

Speed/accuracy trade-off
in pointing tasks



Modern work:

ACT-R (1997)

Cognitive tasks with
visual elements

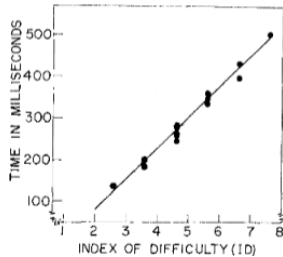


Examples of Cognitive Models

Early work:

Fitt's law (1954)

Speed/accuracy trade-off
in pointing tasks



Modern work:

ACT-R (1997)

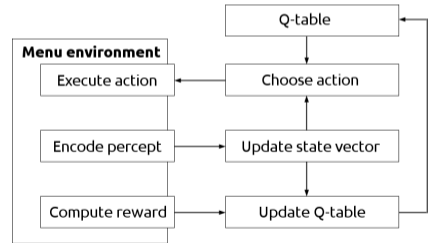
Cognitive tasks with
visual elements



Recent work:

Menu search (CHI 2015)

Visual search in menus

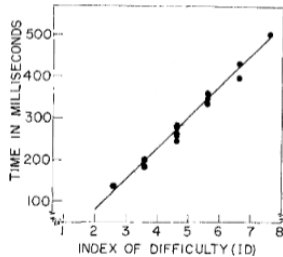


Examples of Cognitive Models

Early work:

Fitt's law (1954)

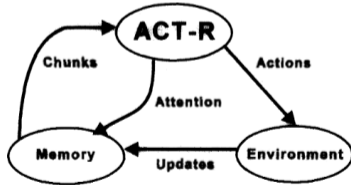
Speed/accuracy trade-off
in pointing tasks



Modern work:

ACT-R (1997)

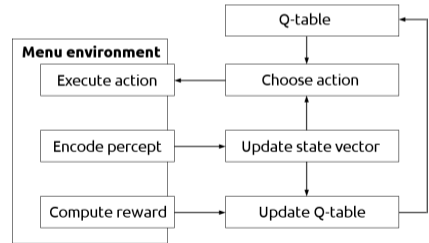
Cognitive tasks with
visual elements



Recent work:

Menu search (CHI 2015)

Visual search in menus



Yesterday: A model of visual decision-making by Chen, Starke, Baber & Howes

Why Model Human Cognition

Why Model Human Cognition

Predicting user behavior



Why Model Human Cognition

Explaining cognitive processes

Predicting user behavior



Why Model Human Cognition

Predicting user behavior



Explaining cognitive processes

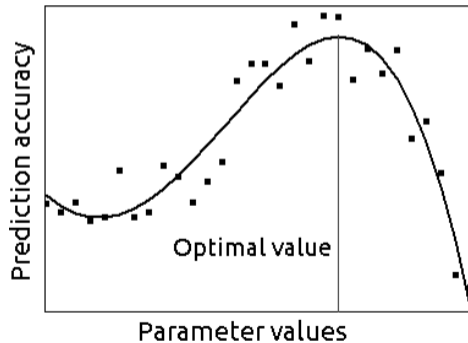


Allowing computer systems to adapt better to the user



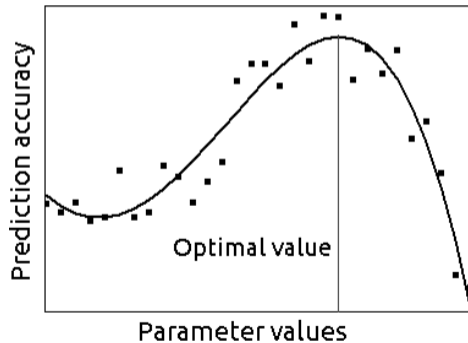
Model Tuning

Goal: select parameters that lead to accurate predictions



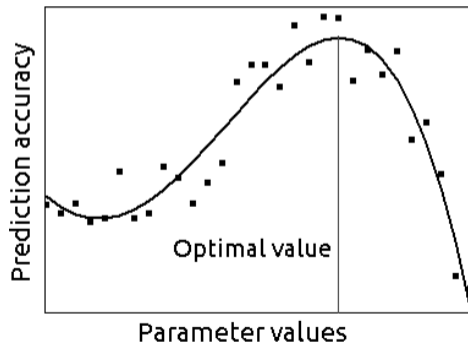
Model Tuning

Goal: select parameters that lead to accurate predictions



Examples of parameters

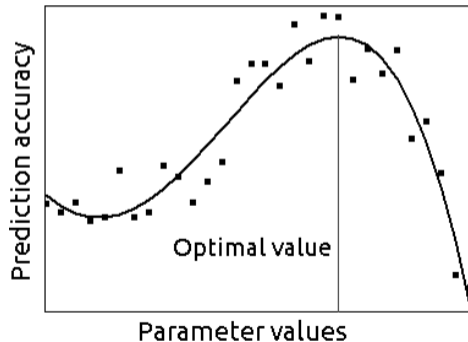
Goal: select parameters that lead to accurate predictions



Examples of parameters

- Duration of a visual fixation

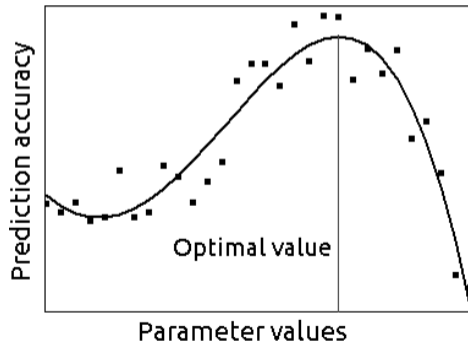
Goal: select parameters that lead to accurate predictions



Examples of parameters

- Duration of a visual fixation
- Acuity and size of peripheral visual field

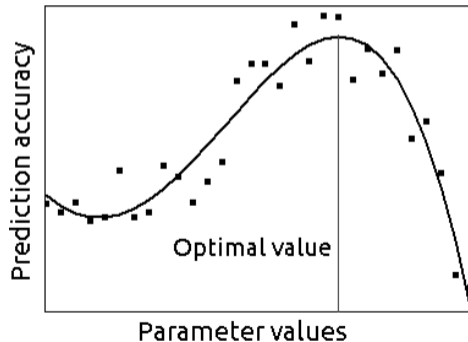
Goal: select parameters that lead to accurate predictions



Examples of parameters

- Duration of a visual fixation
- Acuity and size of peripheral visual field
- Reward for completing the task

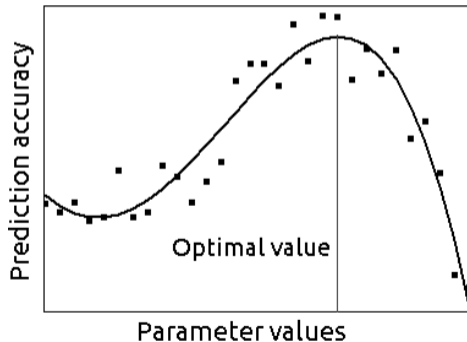
Goal: select parameters that lead to accurate predictions



Examples of parameters

- Duration of a visual fixation
- Acuity and size of peripheral visual field
- Reward for completing the task
- Penalty for wasting one second of time

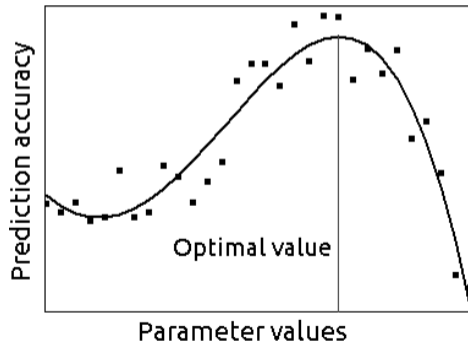
Goal: select parameters that lead to accurate predictions



Examples of parameters

- Duration of a visual fixation
- Acuity and size of peripheral visual field
- Reward for completing the task
- Penalty for wasting one second of time
- Duration of short-term memory

Goal: select parameters that lead to accurate predictions



Examples of parameters

- Duration of a visual fixation
- Acuity and size of peripheral visual field
- Reward for completing the task
- Penalty for wasting one second of time
- Duration of short-term memory
- And so on ..

Characteristics of Modern Cognitive Models

Characteristics of Modern Cognitive Models

No simple way to tune parameters

Highly non-linear model structure, not possible to directly compute best parameter values



Characteristics of Modern Cognitive Models

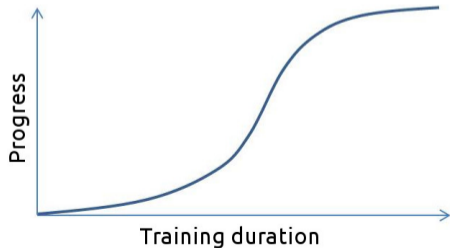
No simple way to tune parameters

Highly non-linear model structure, not possible to directly compute best parameter values



Computing predictions takes time

Once we fix the parameter values, the model needs to first learn a behavior strategy

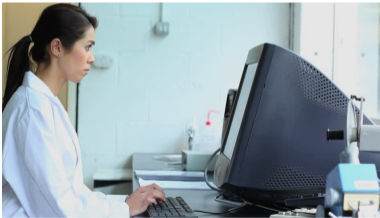


Traditional Tuning Methods

Traditional Tuning Methods

Manual Parameter Tuning

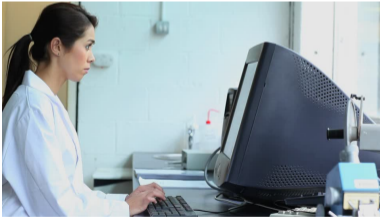
Slow: needs human labour
No guarantees of optimality



Traditional Tuning Methods

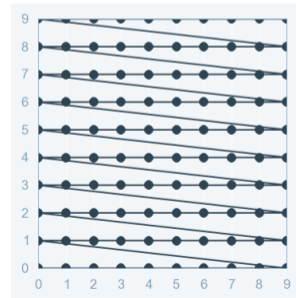
Manual Parameter Tuning

Slow: needs human labour
No guarantees of optimality



Grid search

Might take a very long time
No uncertainty estimates



Approximate Bayesian Computation (ABC)

ABC Inference Process

ABC Inference Process

- Choose parameter values for the model

Approximate Bayesian Computation (ABC)

ABC Inference Process

- Choose parameter values for the model
- Simulate predictions

Approximate Bayesian Computation (ABC)

ABC Inference Process

- Choose parameter values for the model
- Simulate predictions
- Evaluate discrepancy between predictions and observations

Approximate Bayesian Computation (ABC)

ABC Inference Process

- Choose parameter values for the model
- Simulate predictions
- Evaluate discrepancy between predictions and observations
- Use a probabilistic model to estimate discrepancy in different regions of parameter space

Approximate Bayesian Computation (ABC)

ABC Inference Process

- Choose parameter values for the model
- Simulate predictions
- Evaluate discrepancy between predictions and observations
- Use a probabilistic model to estimate discrepancy in different regions of parameter space
- (Repeat until converged)

Approximate Bayesian Computation (ABC)

ABC Inference Process

- Choose parameter values for the model
- Simulate predictions
- Evaluate discrepancy between predictions and observations
- Use a probabilistic model to estimate discrepancy in different regions of parameter space
- (Repeat until converged)

Inference Results

Approximate Bayesian Computation (ABC)

ABC Inference Process

- Choose parameter values for the model
- Simulate predictions
- Evaluate discrepancy between predictions and observations
- Use a probabilistic model to estimate discrepancy in different regions of parameter space
- (Repeat until converged)

Inference Results

- Based on the probabilistic model, we can compute an approximate probability distribution over the parameter space

Approximate Bayesian Computation (ABC)

ABC Inference Process

- Choose parameter values for the model
- Simulate predictions
- Evaluate discrepancy between predictions and observations
- Use a probabilistic model to estimate discrepancy in different regions of parameter space
- (Repeat until converged)

Inference Results

- Based on the probabilistic model, we can compute an approximate probability distribution over the parameter space
- Maximum of the distribution gives us the Maximum Likelihood (ML) estimate

Approximate Bayesian Computation (ABC)

ABC Inference Process

- Choose parameter values for the model
- Simulate predictions
- Evaluate discrepancy between predictions and observations
- Use a probabilistic model to estimate discrepancy in different regions of parameter space
- (Repeat until converged)

Inference Results

- Based on the probabilistic model, we can compute an approximate probability distribution over the parameter space
- Maximum of the distribution gives us the Maximum Likelihood (ML) estimate
- Width of distribution corresponds to uncertainty

Approximate Bayesian Computation (ABC)



Parameter value

Model Predictions

Discrepancy

Observation Data



Approximate Bayesian Computation (ABC)



↑
Parameter value

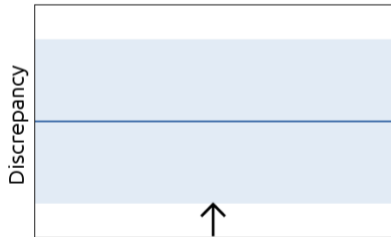
Model Predictions

Discrepancy

Observation Data



Approximate Bayesian Computation (ABC)



Parameter value

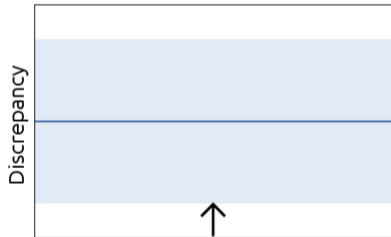
Model Predictions



Discrepancy



Approximate Bayesian Computation (ABC)



↑
Parameter value

Model Predictions



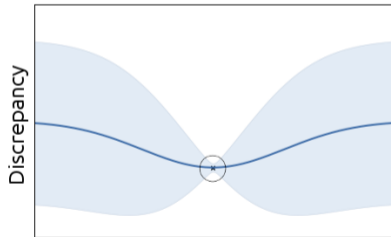
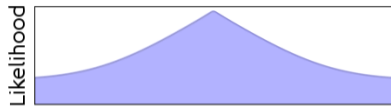
Discrepancy

1.0

Observation Data



Approximate Bayesian Computation (ABC)



Parameter value

Model Predictions



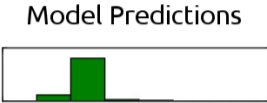
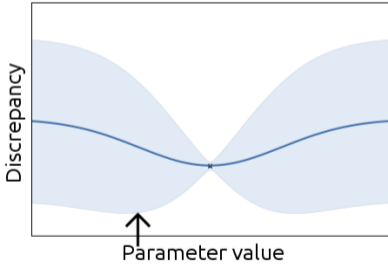
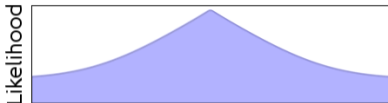
Discrepancy

1.0

Observation Data

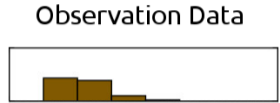


Approximate Bayesian Computation (ABC)

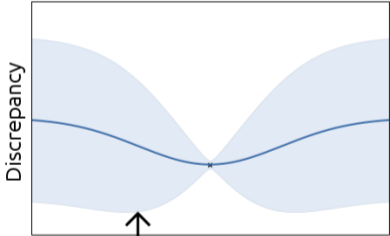
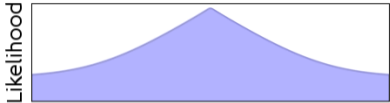


Discrepancy

1.0



Approximate Bayesian Computation (ABC)



Model Predictions



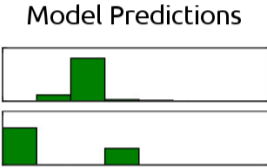
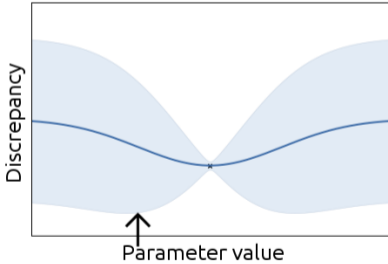
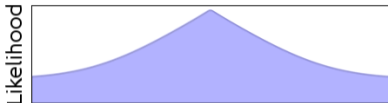
Discrepancy

1.0

Observation Data



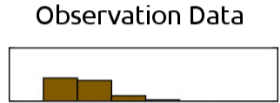
Approximate Bayesian Computation (ABC)



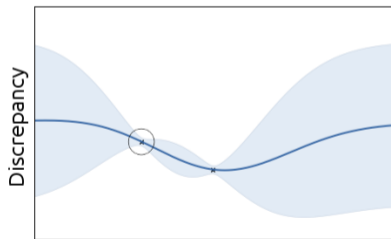
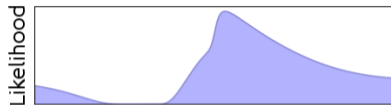
Discrepancy

1.0

1.6

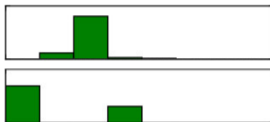


Approximate Bayesian Computation (ABC)



Parameter value

Model Predictions



Discrepancy

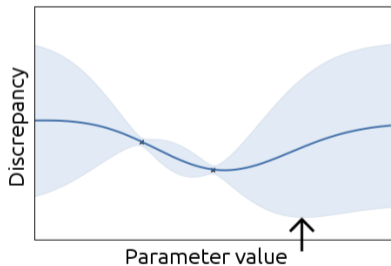
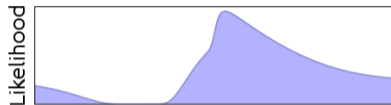
1.0

1.6

Observation Data



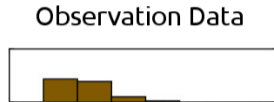
Approximate Bayesian Computation (ABC)



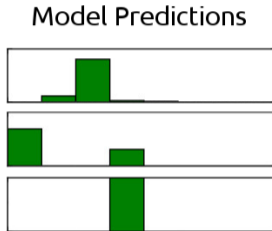
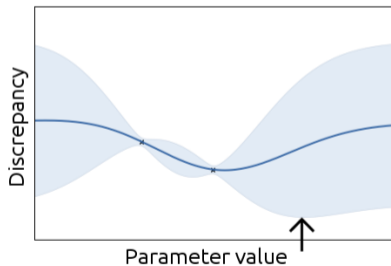
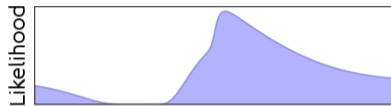
Discrepancy

1.0

1.6



Approximate Bayesian Computation (ABC)



Discrepancy

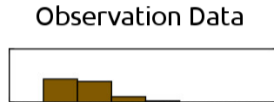
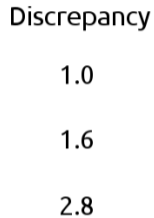
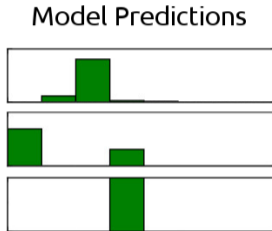
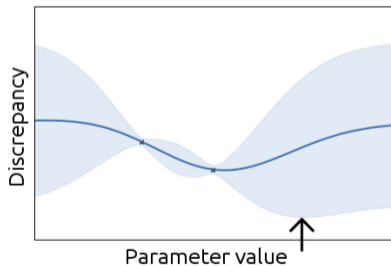
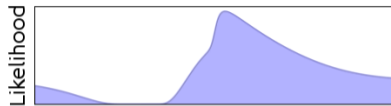
1.0

1.6

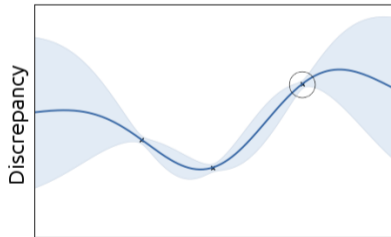
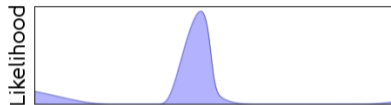
Observation Data



Approximate Bayesian Computation (ABC)

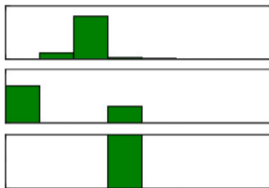


Approximate Bayesian Computation (ABC)



Parameter value

Model Predictions



Discrepancy

1.0

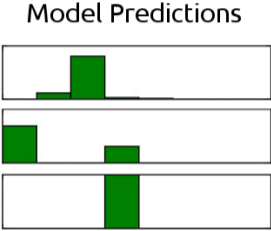
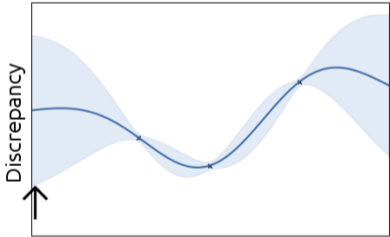
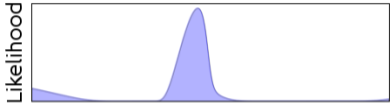
1.6

2.8

Observation Data



Approximate Bayesian Computation (ABC)

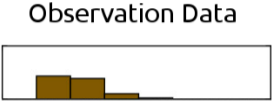


Discrepancy

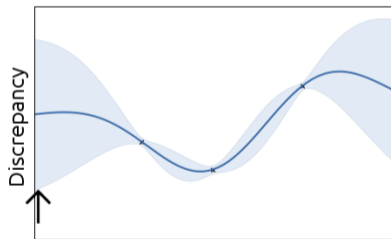
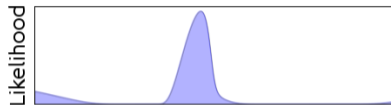
1.0

1.6

2.8

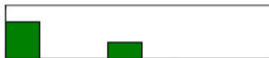


Approximate Bayesian Computation (ABC)



Parameter value

Model Predictions



Discrepancy

1.0

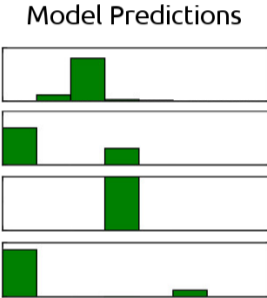
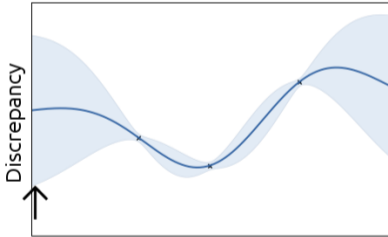
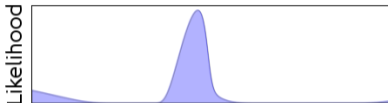
1.6

2.8

Observation Data



Approximate Bayesian Computation (ABC)



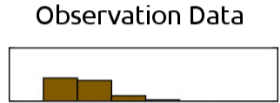
Discrepancy

1.0

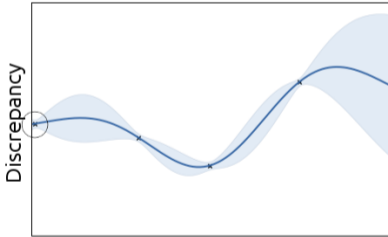
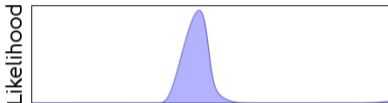
1.6

2.8

1.9

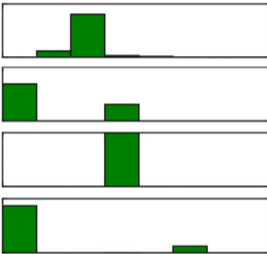


Approximate Bayesian Computation (ABC)



Parameter value

Model Predictions



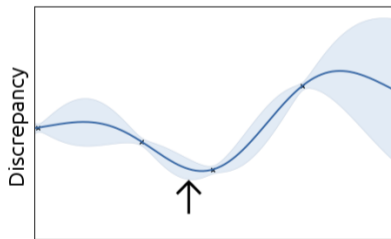
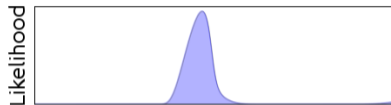
Discrepancy

1.0
1.6
2.8
1.9

Observation Data



Approximate Bayesian Computation (ABC)



Parameter value

Model Predictions



Discrepancy

1.0

1.6

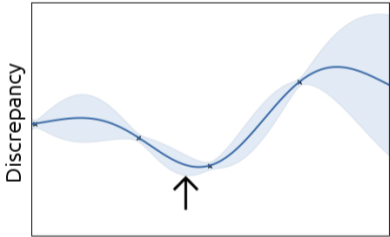
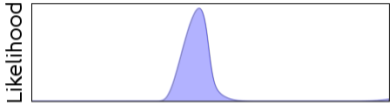
2.8

1.9

Observation Data

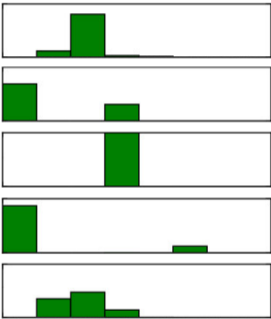


Approximate Bayesian Computation (ABC)



Parameter value

Model Predictions



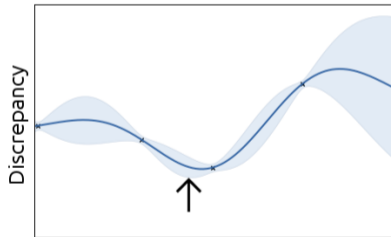
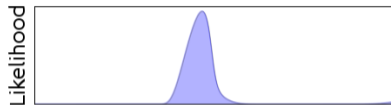
Discrepancy

1.0
1.6
2.8
1.9

Observation Data



Approximate Bayesian Computation (ABC)



Parameter value

Model Predictions



Discrepancy

1.0

1.6

2.8

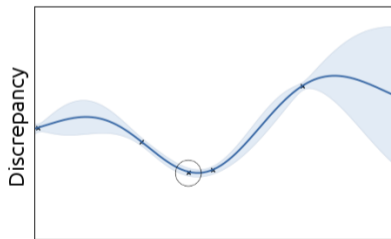
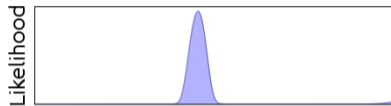
1.9

0.9

Observation Data



Approximate Bayesian Computation (ABC)



Parameter value

Model Predictions



Discrepancy

1.0

1.6

2.8

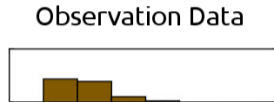
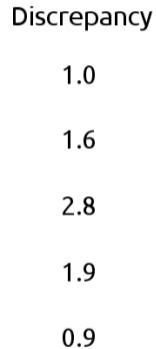
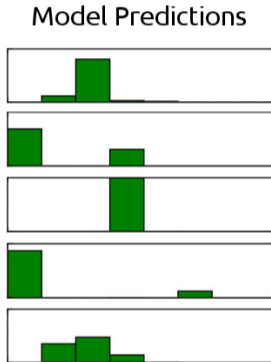
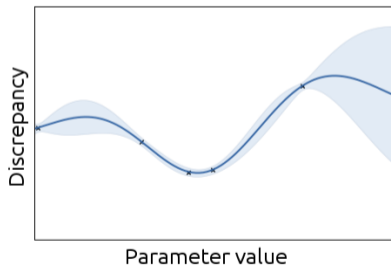
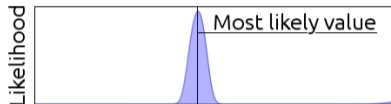
1.9

0.9

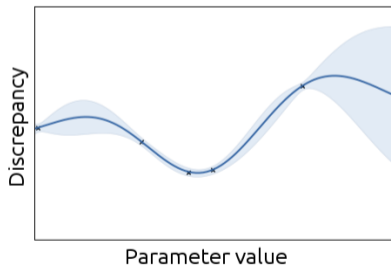
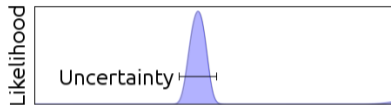
Observation Data



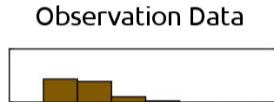
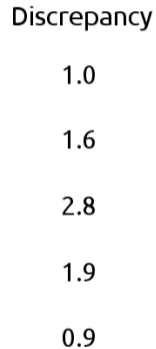
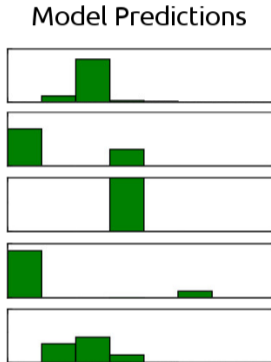
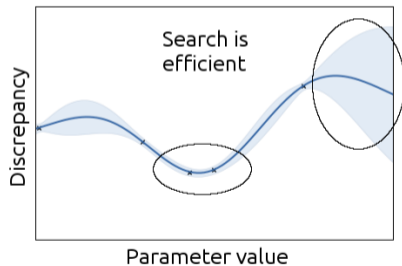
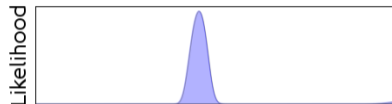
Approximate Bayesian Computation (ABC)



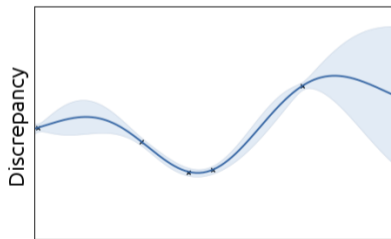
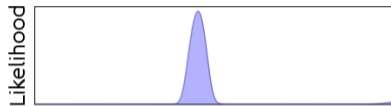
Approximate Bayesian Computation (ABC)



Approximate Bayesian Computation (ABC)

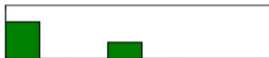


Approximate Bayesian Computation (ABC)



Parameter value

Model Predictions



Discrepancy

1.0

1.6

2.8

1.9

0.9

Observation Data



No special requirements
for observation data

Case Study: Visual Search

Case Study: Visual Search

A recent model for visual search in drop-down menus (Chen *et al.* CHI 2015)



Case Study: Visual Search

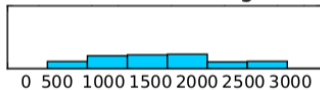
A recent model for visual search in drop-down menus (Chen *et al.* CHI 2015)



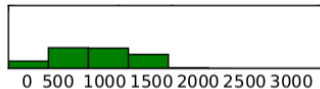
With ABC, the predictions match better to observations

Task Completion Time (ms)

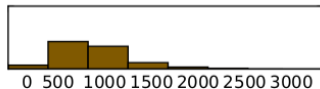
Manual tuning



ABC fitted



Ground truth

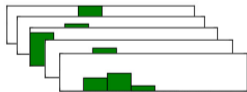


Model Development and Individual Modelling with ABC

Fit different models to same dataset

This allowed us to estimate how different changes to the model affected the predictions

Predictions from Model Variants



Observation Data

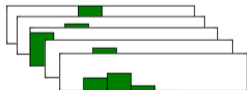


Model Development and Individual Modelling with ABC

Fit different models to same dataset

This allowed us to estimate how different changes to the model affected the predictions

Predictions from Model Variants



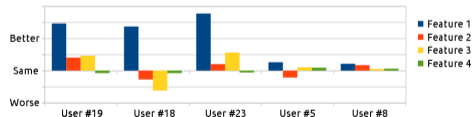
Observation Data



Fit same model to different datasets

By fitting models to observations from individual users we were able to improve the predictions over a population level model

Prediction quality with individual models compared to population level model



Resources for Practical Use of ABC

Requirements for ABC

Requirements for ABC

- A simulator model
(with tunable parameters)

Requirements for ABC

- A simulator model
(with tunable parameters)
- Prior knowledge of
reasonable parameter values

Requirements for ABC

- A simulator model
(with tunable parameters)
- Prior knowledge of
reasonable parameter values
- Observation dataset

Requirements for ABC

- A simulator model
(with tunable parameters)
- Prior knowledge of
reasonable parameter values
- Observation dataset
- Discrepancy measure

Requirements for ABC

- A simulator model
(with tunable parameters)
- Prior knowledge of
reasonable parameter values
- Observation dataset
- Discrepancy measure

Technical Considerations

Requirements for ABC

- A simulator model (with tunable parameters)
- Prior knowledge of reasonable parameter values
- Observation dataset
- Discrepancy measure

Technical Considerations

- There exists programming frameworks for ABC (e.g. ELFI: github.com/elfi-dev/elfi)

Requirements for ABC

- A simulator model (with tunable parameters)
- Prior knowledge of reasonable parameter values
- Observation dataset
- Discrepancy measure

Technical Considerations

- There exists programming frameworks for ABC (e.g. ELFI: github.com/elfi-dev/elfi)
- The more parameters you infer, the more challenging inference is

Requirements for ABC

- A simulator model (with tunable parameters)
- Prior knowledge of reasonable parameter values
- Observation dataset
- Discrepancy measure

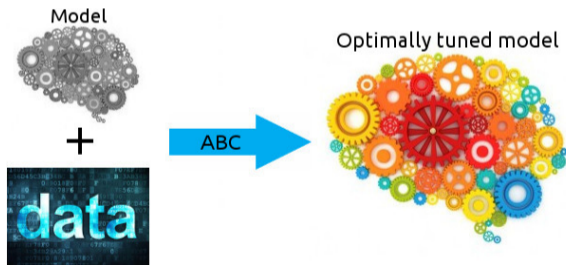
Technical Considerations

- There exists programming frameworks for ABC (e.g. ELFI: github.com/elfi-dev/elfi)
- The more parameters you infer, the more challenging inference is
- Cluster computers offer speedups

Take-home Messages

Tuning the parameters of cognitive models based on real observations is important for making good predictions

Approximate Bayesian Computation (ABC) allows you to do this with only very mild technical requirements



ELFI, a Python library for ABC: github.com/elfi-dev/elfi

Tech paper: Inverse Reinforcement Learning from Summary Data: arxiv.org/abs/1703.09700